

CONCLUSIONS

The main results obtained are:

1. Simulation of convective detonation waves in a porous medium was carried out.

A new model was proposed based on the lattice gas method. This model allows one to take into account the stochastic nature of this phenomenon. Propagation of the wave front and its curved shape were obtained automatically in computations in contrast with existing continual models. Computed wave velocity and pressure profile were in good agreement with experimental ones.

2. Based on the numerical investigation of the component mixing process, a possible mechanism was explained of the time and grain size dependence of electric conductivity in detonation products of heterogeneous HEs.

Flow development for different initial geometry was considered. Time dependencies of detonation product conductivity of heterogeneous HEs were obtained. The dependencies obtained are in qualitative agreement with the experimental results.

3. The modification of the LBE method was developed for simulation of electrohydrodynamic flows. Several methods to compute the convective charge transport were considered. Theoretical values of the numerical diffusivity were compared with the computation results.

Development of EHD-flow in different geometry was studied. In two-dimensional case, the flow has oscillatory character caused by the charge injection in discrete lumps that reduce the electric field. As the voltage between electrodes is increased, the instability of liquid flow emerges which breaks the flow symmetry.

4. For the first time, the possibility of micro-bubble generation in high electric field on the electrode surface by the electrodynamic mechanism was confirmed by direct simulations. At certain conditions, the emergence of a region of gas phase was observed in computations. Such a bubble was

generated in the region of high electric field (near the tip) due to electrodynamic cavitation. The electric breakdown of gas in bubbles generated can further result in the breakdown of liquid.

5. The model was developed which describes the streamer tip propagation and the dynamics of the electric discharge channel expansion in liquid with generation of shock waves. The planar and the cylindrical cases were considered.

The divergent shock waves were observed at the streamer tip propagation with supersonic velocity and at the channel expansion due to energy release inside it.

6. The inner structure of the channel boundary (the transition layer "liquid-plasma") was computed taking into account the liquid viscosity. The non-monotonic pressure variation across the boundary due to viscous tension is shown. Theoretical estimates of the pressure step on the channel boundary and of the pressure peak inside the transition layer agree well with computation results.

Main results were presented on scientific conferences, among them:

- International Symposium on Electrical Insulation (Arlington, 1998)
- 13th and 14th International Conferences on Dielectric Liquids (Nara, 1999, Graz, 2002)
- 2nd International Workshop on Electric Conduction, Convection and Breakdown of Liquids (Grenoble, 2000)
- 12th Symposium on Combustion and Explosion (Chernogolovka, 2000)
- V and VI International Conferences "Modern Problems of Electrophysics and Electrohydrodynamics of Liquids" (Sankt-Petersburg, 1998, 2000)
- II, III, IV and V Siberian Workshops "Mathematical Problems of Fluid Mechanics" (Novosibirsk, 1998, 1999, 2000, 2001)
- International Conference "III Khariton's Topic Scientific Readings" (Sarov, 2001)
- International Conference "VI Zababakhin's Scientific Readings" (Sneginsk, 2001)
- III and IV International Workshops "Pulse Processes in Fluid Mechanics" (Nikolaev, 1999, 2001)

The results obtained are published in [1–14].

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